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ICS 313
Quiz #4
Feb 26, 2009

Quiz #4:

Eliminate left recursion from the following grammar:

$S \rightarrow Ba \mid Ab$
 $A \rightarrow Sa \mid AAb \mid a$
 $B \rightarrow Sb \mid BBa \mid b$

a. In the order of B, S, A:

$B \rightarrow Sb \mid BBa \mid b$
 $S \rightarrow Ba \mid Ab$
 $A \rightarrow Sa \mid AAb \mid a$

Solving...

$B \rightarrow Sb \mid BBa \mid b$

$\Rightarrow \alpha_1 = Ba$
 $\beta_1 = Sb$
 $\beta_2 = b$
 $\Rightarrow B \rightarrow Sb \mid b \mid SbP \mid bP$
 $P \rightarrow Ba \mid BaP$

$S \rightarrow Ba \mid Ab$
 $\rightarrow Sba \mid ba \mid SbPa \mid bPa \mid Ab$

$\Rightarrow \alpha_1 = ba$
 $\alpha_2 = bPa$
 $\beta_1 = ba$
 $\beta_2 = bPa$
 $\beta_3 = Ab$

$$\begin{aligned} \Rightarrow S &\rightarrow ba \mid bPa \mid Ab \mid baQ \mid bPaQ \mid AbQ \\ Q &\rightarrow ba \mid bPa \mid baQ \mid bPaQ \\ \\ A &\rightarrow Sa \mid AAb \mid a \\ &\rightarrow baa \mid bPaa \mid Aba \mid baQa \mid bPaQa \mid AbQa \mid AAb \mid a \\ \\ \Rightarrow \alpha_1 &= ba \\ \alpha_2 &= bQa \\ \alpha_3 &= Ab \\ \beta_1 &= baa \\ \beta_2 &= bPaa \\ \beta_3 &= baQa \\ \beta_4 &= bPaQa \\ \beta_5 &= a \\ \Rightarrow A &\rightarrow baa \mid bPaa \mid baQa \mid bPaQa \mid a \mid \\ &\quad baaR \mid bPaaR \mid baQaR \mid bPaQaR \mid aR \\ R &\rightarrow ba \mid bQa \mid Ab \mid baR \mid bQaR \mid AbR \end{aligned}$$

Solution:

$$\begin{aligned} B &\rightarrow Sb \mid b \mid SbP \mid bP \\ P &\rightarrow Ba \mid BaP \\ S &\rightarrow ba \mid bPa \mid Ab \mid baQ \mid bPaQ \mid AbQ \\ Q &\rightarrow ba \mid bPa \mid baQ \mid bPaQ \\ A &\rightarrow baa \mid bPaa \mid baQa \mid bPaQa \mid a \mid \\ &\quad baaR \mid bPaaR \mid baQaR \mid bPaQaR \mid aR \\ R &\rightarrow ba \mid bQa \mid Ab \mid baR \mid bQaR \mid AbR \end{aligned}$$

b. In the order of S, A, B

$$\begin{aligned} S &\rightarrow Ba \mid Ab \\ A &\rightarrow Sa \mid AAb \mid a \\ B &\rightarrow Sb \mid BBa \mid b \end{aligned}$$

Solving...

$$\begin{aligned} A &\rightarrow Sa \mid AAb \mid a \\ &\rightarrow Baa \mid Aba \mid AAb \mid a \end{aligned}$$

\Rightarrow $\alpha_1 = ba$
 $\alpha_2 = Ab$
 $\beta_1 = Baa$
 $\beta_2 = a$

\Rightarrow $A \rightarrow Baa \mid a \mid BaaP \mid aP$
 $P \rightarrow ba \mid Ab \mid baP \mid AbP$

$B \rightarrow Sb \mid BBa \mid b$
 $\rightarrow Bab \mid Abb \mid BBa \mid b$
 $\rightarrow Bab \mid Baabb \mid abb \mid BaaPbb \mid aPbb \mid BBa \mid b$

\Rightarrow $\alpha_1 = ab$
 $\alpha_2 = aabb$
 $\alpha_3 = aaPbb$
 $\alpha_4 = Ba$
 $\beta_1 = abb$
 $\beta_2 = aPbb$
 $\beta_3 = b$

\Rightarrow $B \rightarrow abb \mid aPbb \mid b \mid abbQ \mid aPbbQ \mid bQ$
 $Q \rightarrow ab \mid aabb \mid aaPbb \mid abQ \mid aabbQ \mid aaPbbQ$

Solution:

$S \rightarrow Ba \mid Ab$
 $A \rightarrow Baa \mid a \mid BaaP \mid aP$
 $P \rightarrow ba \mid Ab \mid baP \mid AbP$
 $B \rightarrow abb \mid aPbb \mid b \mid abbQ \mid aPbbQ \mid bQ$
 $Q \rightarrow ab \mid aabb \mid aaPbb \mid abQ \mid aabbQ \mid aaPbbQ$